# Stephen T. ThorntonAndrew RexModern Physicsfor Scientists and Engineers

Fourth Edition

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Fundamental Constants		
Quantity	Symbol	Value(s)
Elementary charge	e	$1.6022  imes 10^{-19} \mathrm{C}$
Speed of light in vacuum	С	$2.9979 imes10^8~{ m m/s}$
Permeability of vacuum (magnetic constant)	$\mu_0$	$4\pi  imes 10^{-7} \mathrm{N} \cdot \mathrm{A}^{-2}$
Permittivity of vacuum (electric constant)	$\epsilon_0$	$8.8542  imes 10^{-12}  \mathrm{F} \cdot \mathrm{m}^{-1}$
Gravitation constant	G	$6.6738  imes 10^{-11} \mathrm{N \cdot m^2 \cdot kg^{-2}}$
Planck constant	h	$6.6261  imes 10^{-34} \mathrm{J}\cdot\mathrm{s}$
		$4.1357\times 10^{-15}~{\rm eV}\cdot{\rm s}$
Avogadro constant	$N_{\mathrm{A}}$	$6.0221  imes 10^{23}  \mathrm{mol^{-1}}$
Boltzmann constant	k	$1.3807  imes 10^{-23} \mathrm{J} \cdot \mathrm{K}^{-1}$
Stefan-Boltzmann constant	$\sigma$	$5.6704  imes 10^{-8} \mathrm{W} \cdot \mathrm{m}^{-2} \cdot \mathrm{K}^{-4}$
Atomic mass unit	u	$\frac{1.66053886\times10^{-27}\mathrm{kg}}{931.494061~\mathrm{MeV}/c^2}$

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	Mass in units of			
Particle	kg	MeV/c <sup>2</sup>	u	
Electron	$9.1094  imes 10^{-31}$	0.51100	$5.4858\times10^{-4}$	
Muon	$1.8835  imes 10^{-28}$	105.66	0.11343	
Proton	$1.6726  imes 10^{-27}$	938.27	1.00728	
Neutron	$1.6749  imes 10^{-27}$	939.57	1.00866	
Deuteron	$3.3436  imes 10^{-27}$	1875.61	2.01355	
$\alpha$ particle	$6.6447  imes 10^{-27}$	3727.38	4.00151	

## Conversion Factors

$1 \text{ y} = 3.156 \times 10^7 \text{ s}$
1 lightyear = $9.461 \times 10^{15}$ m
1  cal = 4.186  J
$1~{\rm MeV}/c = 5.344 \times 10^{-22}~{\rm kg}\cdot{\rm m/s}$
$1 \text{ eV} = 1.6022 \times 10^{-19} \text{ J}$

1 T = 10<sup>4</sup> G 1 Ci =  $3.7 \times 10^{10}$  Bq 1 barn =  $10^{-28}$  m<sup>2</sup> 1 u =  $1.66054 \times 10^{-27}$  kg

#### Useful Combinations of Constants

 $\hbar = h/2\pi = 1.0546 \times 10^{-34}$  J · s = 6.5821 × 10<sup>-16</sup> eV · s  $hc = 1.9864 \times 10^{-25} \text{ J} \cdot \text{m} = 1239.8 \text{ eV} \cdot \text{nm}$  $\hbar c = 3.1615 \times 10^{-26} \text{ J} \cdot \text{m} = 197.33 \text{ eV} \cdot \text{nm}$  $\frac{1}{4\pi\epsilon_0} = 8.9876 \times 10^9 \,\mathrm{N} \cdot \mathrm{m}^2 \cdot \mathrm{C}^{-2}$ Compton wavelength  $\lambda_c = \frac{h}{m_c c} = 2.4263 \times 10^{-12} \text{ m}$  $\frac{e^2}{4\pi\epsilon_0} = 2.3071 \times 10^{-28} \text{J} \cdot \text{m} = 1.4400 \times 10^{-9} \text{ eV} \cdot \text{m}$ Fine structure constant  $\alpha = \frac{e^2}{4\pi\epsilon_0\hbar c} = 0.0072974 \approx \frac{1}{137}$ Bohr magneton  $\mu_{\rm B} = \frac{e\hbar}{2m_e} = 9.2740 \times 10^{-24} \,\text{J/T} = 5.7884 \times 10^{-5} \,\text{eV/T}$ Nuclear magneton  $\mu_{\rm N} = \frac{e\hbar}{2m_{\rm p}} = 5.0508 \times 10^{-27} \,{\rm J/T}$ =  $3.1525 \times 10^{-8} \,{\rm eV/T}$ Bohr radius  $a_0 = \frac{4\pi\epsilon_0\hbar^2}{m_e e^2} = 5.2918 \times 10^{-11} \,\mathrm{m}$ Hydrogen ground state  $E_0 = \frac{e^2}{8\pi\epsilon_0 a_0} = 13.606 \text{ eV} = 2.1799 \times 10^{-18} \text{ J}$ Rydberg constant  $R_{\infty} = \frac{\alpha^2 m_e c}{2h} = 1.09737 \times 10^7 \,\mathrm{m}^{-1}$ Hydrogen Rydberg  $R_{\rm H} = \frac{\mu}{m_{\star}} R_{\infty} = 1.09678 \times 10^7 \, {\rm m}^{-1}$ Gas constant  $R = N_A k = 8.3145 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ Magnetic flux quantum  $\Phi_0 = \frac{h}{2e} = 2.0678 \times 10^{-15} \,\mathrm{T} \cdot \mathrm{m}^2$ Classical electron radius  $r_e = \alpha^2 a_0 = 2.8179 \times 10^{-15} \text{ m}$  $kT = 2.5249 \times 10^{-2} \text{ eV} \approx \frac{1}{40} \text{ eV} \text{ at } T = 293 \text{ K}$ 

*Note:* The latest values of the fundamental constants can be found at the National Institute of Standards and Technology website at http://physics.nist.gov/cuu/Constants



# MODERN PHYSICS

# For Scientists and Engineers

Fourth Edition

# STEPHEN T. THORNTON

University of Virginia

# ANDREW REX

University of Puget Sound



Australia • Brazil • Japan • Korea • Mexico • Singapore • Spain • United Kingdom • United States

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#### Modern Physics for Scientists and Engineers, Fourth Edition Stephen T. Thornton, Andrew Rex

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Text design: Reuter Designs

Cover design: Gary Regaglia, Metro Design

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Library of Congress Control Number: 2011926934 Student Edition: ISBN-13: 978-1-133-10372-1

ISBN-10: 1-133-10372-3

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Printed in the United States of America 1 2 3 4 5 6 7 15 14 13 12 11



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# Preface

Our objective in writing this book was to produce a textbook for a modern physics course of either one or two semesters for physics and engineering students. Such a course normally follows a full-year, introductory, calculus-based physics course for freshmen or sophomores. Before each edition we have the publisher send a questionnaire to users of modern physics books to see what needed to be changed or added. Most users like our textbook as is, especially the complete coverage of topics including the early quantum theory, subfields of physics, general relativity, and cosmology/astrophysics. Our book continues to be useful for either a one- or two-semester modern physics course. We have made no major changes in the order of subjects in the fourth edition.

#### Coverage

The first edition of our text established a trend for a contemporary approach to the exciting, thriving, and changing field of modern science. After briefly visiting the status of physics at the turn of the last century, we cover relativity and quantum theory, the basis of any study of modern physics. Almost all areas of science depend on quantum theory and the methods of experimental physics. We have included the name Quantum Mechanics in two of our chapter titles (Chapters 5 and 6) to emphasize the quantum connection. The latter part of the book is devoted to the subfields of physics (atomic, condensed matter, nuclear, and particle) and the exciting fields of cosmology and astrophysics. Our experience is that science and engineering majors particularly enjoy the study of modern physics after the sometimes-laborious study of classical mechanics, thermodynamics, electricity, magnetism, and optics. The level of mathematics is not difficult for the most part, and students feel they are finally getting to the frontiers of physics. We have brought the study of modern physics alive by presenting many current applications and challenges in physics, for example, nanoscience, high-temperature superconductors, quantum teleportation, neutrino mass and oscillations, missing dark mass and energy in the universe, gamma-ray bursts, holography, quantum dots, and nuclear fusion. Modern physics texts need to be updated periodically to include recent advances. Although we have emphasized modern applications, we also provide the sound theoretical basis for quantum theory that will be needed by physics majors in their upper division and graduate courses.

#### **Changes for the Fourth Edition**

Our book continues to be the most complete and up-to-date textbook in the modern physics market for sophomores/juniors. We have made several changes for the fourth edition to aid the student in learning modern physics. We have added additional end-of-chapter questions and problems and have modified many problems from earlier editions,

with an emphasis on including more real-world problems with current research applications whenever possible. We continue to have a larger number of questions and problems than competing textbooks, and for users of the robust Thornton/Rex *Modern Physics for Scientists and Engineers*, third edition course in WebAssign, we have a correlation guide of the fourth edition problems to that third edition course.

We have added additional examples to the already large number in the text. The pedagogical changes made for the third edition were highly successful. To encourage and support conceptual thinking by students, we continue to use conceptual examples and strategy discussion in the numerical examples. Examples with numerical solutions include a discussion of what needs to be accomplished in the example, the procedure to go through to find the answer, and relevant equations that will be needed. We present the example solutions in some detail, showing enough steps so that students can follow the solution to the end.

We continue to provide a significant number of photos and biographies of scientists who have made contributions to modern physics. We have done this to give students a perspective of the background, education, trials, and efforts of these scientists. We have also updated many of the Special Topic boxes, which we believe provide accurate and useful descriptions of the excitement of scientific discoveries, both past and current.

**Chapter-by-Chapter Changes** We have rewritten some sections in order to make the explanations clearer to the student. Some material has been deleted, and new material has been added. In particular we added new results that have been reported since the third edition. This is especially true for the chapters on the subfields of physics, Chapters 8–16. We have covered the most important subjects of modern physics, but we realize that in order to cover everything, the book would have to be much longer, which is not what our users want. Our intention is to keep the level of the textbook at the sophomore/junior undergraduate level. We think it is important for instructors to be able to supplement the book whenever they choose—especially to cover those topics in which they themselves are expert. Particular changes by chapter include the following:

- **Chapter 2:** we have updated the search for violations of Lorentz symmetry and added some discussion about four vectors.
- **Chapter 3:** we have rewritten the discussion of the Rayleigh-Jeans formula and Planck's discovery.
- **Chapter 9:** we improved the discussion about the symmetry of boson wave functions and its application to the Fermi exclusion principle and Bose-Einstein condensates.
- Chapter 10: we added a discussion of classes of superconductors and have updated our discussion concerning applications of superconductivity. The latter includes how superconductors are now being used to determine several fundamental constants.
- **Chapter 11:** we added more discussion about solar energy, Blu-ray DVD devices, increasing the number of transistors on a microchip using new semiconductor materials, graphene, and quantum dots. Our section on nanotechnology is especially complete.
- **Chapter 12:** we updated our discussion on neutrino detection and neutrino mass, added a description of nuclear magnetic resonance, and upgraded our discussion on using radioactive decay to study the oldest terrestrial materials.
- Chapter 13: we updated our discussion about nuclear power plants operating in the United States and the world and presented a discussion of possible new, improved reactors. We discussed the tsunami-induced tragedy at the Fukushima Daiichi nuclear power plant in Japan and added to our discussion of searches for new elements and their discoveries.
- **Chapter 14:** we upgraded our description of particle physics, improved and expanded the discussion on Feynman diagrams, updated the search for the Higgs boson, discussed new experiments on neutrino oscillations, and added discussion on matter-antimatter, supersymmetry, string theory, and M-theory. We mention that the LHC has begun operation as the Fermilab Tevatron accelerator is shutting down.
- **Chapter 15:** we improved our discussion on gravitational wave detection, added to our discussion on black holes, and included the final results of the Gravity Probe B satellite.

• **Chapter 16:** we changed the chapter name from Cosmology to Cosmology and Modern Astrophysics, because of the continued importance of the subject in modern physics. Our third edition of the textbook already had an excellent discussion and correct information about the age of the universe, dark matter, and dark energy, but Chapter 16 still has the most changes of any chapter, due to the current pace of research in the field. We have upgraded information and added discussion about Olbers' paradox, discovery of the cosmic microwave background, gamma ray astrophysics, standard model of cosmology, the future of space telescopes, and the future of the universe (Big Freeze, Big Crunch, Big Rip, Big Bounce, etc).

## **Teaching Suggestions**

The text has been used extensively in its first three editions in courses at our home institutions. These include a one-semester course for physics and engineering students at the University of Virginia and a two-semester course for physics and pre-engineering students at the University of Puget Sound. These are representative of the one- and two-semester modern physics courses taught elsewhere. Both one- and two-semester courses should cover the material through the establishment of the periodic table in Chapter 8 with few exceptions. We have eliminated the denoting of optional sections, because we believe that depends on the wishes of the instructor, but we feel Sections 2.4, 4.2, 6.4, 6.6, 7.2, 7.6, 8.2, and 8.3 from the first nine chapters might be optional. Our suggestions for the one- and two-semester courses (3 or 4 credit hours per semester) are then

**One-semester:** Chapters 1–9 and selected other material as chosen by the instructor

**Two-semester:** Chapters 1–16 with supplementary material as desired, with possible student projects

An Internet-based, distance-learning version of the course is offered by one of the authors every summer (Physics 2620, 4 credit hours) at the University of Virginia that covers all chapters of the textbook, with emphasis on Chapters 1–8. Homework problems and exams are given on WebAssign. The course can be taken by a student located anywhere there is an Internet connection. See http://modern.physics.virginia.edu/course/ for details.

#### **Features**

#### **End-of-Chapter Problems**

The 1166 questions and problems (258 questions and 908 problems) are more than in competing textbooks. Such a large number of questions and problems allows the instructor to make different homework assignments year after year without having to repeat problems. A correlation guide to the Thornton/Rex *Modern Physics for Scientists and Engineers*, third edition course in WebAssign is available via the Instructor's companion website (www.cengage.com/physics/thornton4e). We have tried to provide thought-provoking questions that have actual answers. In this edition we have focused on adding problems that have real-world or current research applications. The end-of-chapter problems have been separated by section, and general problems are included at the end to allow assimilation of the material. The easier problems are generally listed first within a section, and the more difficult ones are noted by a shaded blue square behind the problem number. A few computer-based problems are given in the text, but no computer disk supplement is provided, because many computer software programs are commercially available.

#### **Solutions Manuals**

PDF files of the *Instructor's Solutions Manual* are available to the instructor on the *Instructor's Resource CD-ROM* (by contacting your local Brooks/Cole—Cengage sales representative). This manual contains the *solution to every end-of-chapter problem* and has been checked by at

least two physics professors. The answers to selected odd-numbered problems are given at the end of the textbook itself. A *Student Solutions Manual* that contains the solutions to about 25% of the end-of-chapter problems is also available for sale to the students.

#### Instructor's Resource CD-ROM for Thornton/Rex's Modern Physics

#### for Scientists and Engineers, Fourth Edition

Available to adopters is the *Modern Physics for Scientists and Engineers Instructor's Resource CD-ROM*. This CD-ROM includes PowerPoint<sup>®</sup> lecture outlines and also contains 200 pieces of line art from the text. It also features PDF files of the *Instructor's Solutions Manual*. Please guard this CD and do not let anyone have access to it. When end-of-chapter problem solutions find their way to the internet for sale, learning by students deteriorates because of the temptation to look up the solution.

#### **Text Format**

The two-color format helps to present clear illustrations and to highlight material in the text; for example, important and useful equations are highlighted in blue, and the most important part of each illustration is rendered in thick blue lines. Blue margin notes help guide the student to the important points, and the margins allow students to make their own notes. The first time key words or topics are introduced they are set in **boldface**, and *italics* are used for emphasis.

#### **Examples**

Although we had a large number of worked examples in the third edition, we have added new ones in this edition. The examples are written and presented in the manner in which students are expected to work the end-of-chapter problems: that is, to develop a conceptual understanding and strategy before attempting a numerical solution. Problem solving does not come easily for most students, especially the problems requiring several steps (that is, not simply plugging numbers into one equation). We expect that the many text examples with varying degrees of difficulty will help students.

#### **Special Topic Boxes**

Users have encouraged us to keep the Special Topic boxes. We believe both students and professors find them interesting, because they add some insight and detail into the excitement of physics. We have updated the material to keep them current.

#### **History**

We include historical aspects of modern physics that some students will find interesting and that others can simply ignore. We continue to include photos and biographies of scientists who have made significant contributions to modern physics. We believe this helps to enliven and humanize the material.

#### Website

Students can access the book's companion website at www.cengagebrain.com/shop/ ISBN/9781133103721. This site features student study aids such as outlines, summaries, and conceptual questions for each chapter. Instructors will also find downloadable PowerPoint lectures and images for use in classroom lecture presentation. Students may also access the authors' websites at http://www.modern.physics.virginia.edu/ and http://www. pugetsound.edu/faculty-pages/rex where the authors will post errata, present new exciting results, and give links to sites that have particularly interesting features like simulations and photos, among other things.



## Acknowledgments

We acknowledge the assistance of many persons who have helped with this text. There are too many that helped us with the first three editions to list here, but the book would not have been possible without them. We acknowledge the professional staff at Brooks/Cole, Cengage Learning who helped make this fourth edition a useful, popular, and attractive text. They include Developmental Editor Ed Dodd and Senior Content Project Manager Cathy Brooks, who kept the production process on track, and Physics Publisher Charlie Hartford for his support, guidance, and encouragement. Elizabeth Budd did a superb job with the copyediting. We also want to thank Jeff Somers and the staff of Graphic World Inc. for their skilled efforts. We also want to thank the many individuals who gave us critical reviews and suggestions since the first edition. We especially would like to thank Michael Hood (Mt. San Antonio College) and Carol Hood (Augusta State University) for their help, especially with the Cosmology and Modern Astrophysics chapter. In preparing this fourth edition, we owe a special debt of gratitude to the following reviewers:

Jose D'Arruda, University of North Carolina, Pembroke David Church, Texas A & M University Hardin R. Dunham, Odessa College Paul A. Heiney, University of Pennsylvania Paul Keyes, Wayne State University Cody Martin, College of Menominee Nation

Prior to our work on this revision, we conducted a survey of professors to gauge how they taught their classes. In all, 78 professors responded with many insightful comments, and we would like to thank them for their feedback and suggestions.

We especially want to acknowledge the valuable help of Richard R. Bukrey of Loyola University of Chicago who helped us in many ways through his enlightening reviews, careful manuscript proofing, and checking of the end-of-chapter problem solutions in the first two editions, and to Thushara Perera of Illinois Wesleyan University, and Paul Weber of University of Puget Sound, for their accuracy review of the fourth edition. We also thank Allen Flora of Hood College for assuming the task of preparing and checking problem solutions for the third and fourth editions.

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# The Birth of Modern Physics

The more important fundamental laws and facts of physical science have all been discovered, and these are now so firmly established that the possibility of their ever being supplanted in consequence of new discoveries is exceedingly remote. . . . Our future discoveries must be looked for in the sixth place of decimals.

Albert A. Michelson, 1894

There is nothing new to be discovered in physics now. All that remains is more and more precise measurement.

William Thomson (Lord Kelvin), 1900

A lthough the Greek scholars Aristotle and Eratosthenes performed measurements and calculations that today we would call physics, the discipline of physics has its roots in the work of Galileo and Newton and others in the scientific revolution of the sixteenth and seventeenth centuries. The knowledge and practice of physics grew steadily for 200 to 300 years until another revolution in physics took place, which is the subject of this book. Physicists distinguish *classical physics*, which was mostly developed before 1895, from *modern physics*, which is based on discoveries made after 1895. The precise year is unimportant, but monumental changes occurred in physics around 1900.

The long reign of Queen Victoria of England, from 1837 to 1901, saw considerable changes in social, political, and intellectual realms, but perhaps none so important as the remarkable achievements that occurred in physics. For example, the description and predictions of electromagnetism by Maxwell are partly responsible for the rapid telecommunications of today. It was also during this period that thermodynamics rose to become an exact science. None of these achievements, however, have had the ramifications of the discoveries and applications of modern physics that would occur in the twentieth century. The world would never be the same.

In this chapter we briefly review the status of physics around 1895, including Newton's laws, Maxwell's equations, and the laws of thermodynamics. These results are just as important today as they were over a hundred years ago. Arguments by scientists concerning the interpretation of experimental data using СНАРТЕК



wave and particle descriptions that seemed to have been resolved 200 years ago were reopened in the twentieth century. Today we look back on the evidence of the late nineteenth century and wonder how anyone could have doubted the validity of the atomic view of matter. The fundamental interactions of gravity, electricity, and magnetism were thought to be well understood in 1895. Physicists continued to be driven by the goal of understanding fundamental laws throughout the twentieth century. This is demonstrated by the fact that other fundamental forces (specifically the nuclear and weak interactions) have been added, and in some cases—curious as it may seem—various forces have even been combined. The search for the holy grail of fundamental interactions continues unabated today.

We finish this chapter with a status report on physics just before 1900. The few problems not then understood would be the basis for decades of fruitful investigations and discoveries continuing into the twenty-first century. We hope you find this chapter interesting both for the physics presented and for the historical account of some of the most exciting scientific discoveries of the modern era.

# **1.1 Classical Physics of the 1890s**

Scientists and engineers of the late nineteenth century were indeed rather smug. They thought they had just about everything under control (see the quotes from Michelson and Kelvin on page 1). The best scientists of the day were highly recognized and rewarded. Public lectures were frequent. Some scientists had easy access to their political leaders, partly because science and engineering had benefited their war machines, but also because of the many useful technical advances. Basic research was recognized as important because of the commercial and military applications of scientific discoveries. Although there were only primitive automobiles and no airplanes in 1895, advances in these modes of transportation were soon to follow. A few people already had telephones, and plans for widespread distribution of electricity were under way.

Based on their success with what we now call macroscopic classical results, scientists felt that given enough time and resources, they could explain just about anything. They did recognize some difficult questions they still couldn't answer; for example, they didn't clearly understand the structure of matter—that was under intensive investigation. Nevertheless, on a macroscopic scale, they knew how to build efficient engines. Ships plied the lakes, seas, and oceans of the world. Travel between the countries of Europe was frequent and easy by train. Many scientists were born in one country, educated in one or two others, and eventually worked in still other countries. The most recent ideas traveled relatively quickly among the centers of research. Except for some isolated scientists, of whom Einstein is the most notable example, discoveries were quickly and easily shared. Scientific journals were becoming accessible.

The ideas of classical physics are just as important and useful today as they were at the end of the nineteenth century. For example, they allow us to build automobiles and produce electricity. The conservation laws of energy, linear momentum, angular momentum, and charge can be stated as follows:

**Classical conservation laws** 

**Conservation of energy:** The total sum of energy (in all its forms) is conserved in all interactions.

**Conservation of linear momentum:** In the absence of external forces, linear momentum is conserved in all interactions (vector relation).

**Early successes of science** 

**Conservation of angular momentum:** In the absence of external torque, angular momentum is conserved in all interactions (vector relation).

Conservation of charge: Electric charge is conserved in all interactions.

A nineteenth-century scientist might have added the **conservation of mass** to this list, but we know it not to be valid today (you will find out why in Chapter 2). These conservation laws are reflected in the laws of mechanics, electromagnetism, and thermodynamics. Electricity and magnetism, separate subjects for hundreds of years, were combined by James Clerk Maxwell (1831–1879) in his four equations. Maxwell showed optics to be a special case of electromagnetism. Waves, which permeated mechanics and optics, were known to be an important component of nature. Many natural phenomena could be explained by wave motion using the laws of physics.

#### **Mechanics**

The laws of mechanics were developed over hundreds of years by many researchers. Important contributions were made by astronomers because of the great interest in the heavenly bodies. Galileo (1564–1642) may rightfully be called the first great experimenter. His experiments and observations laid the groundwork for the important discoveries to follow during the next 200 years.

Isaac Newton (1642–1727) was certainly the greatest scientist of his time and one of the best the world has ever seen. His discoveries were in the fields of mathematics, astronomy, and physics and include gravitation, optics, motion, and forces.

We owe to Newton our present understanding of motion. He understood clearly the relationships among position, displacement, velocity, and acceleration. He understood how motion was possible and that a body at rest was just a special case of a body having constant velocity. It may not be so apparent to us today, but we should not forget the tremendous unification that Newton made when he pointed out that the motions of the planets about our sun can be understood by the same laws that explain motion on Earth, like apples falling from trees or a soccer ball being shot toward a goal. Newton was able to elucidate Galileo, the first great experimenter

Newton, the greatest scientist of his time

Galileo Galilei (1564–1642) was born, educated, and worked in Italy. Often said to be the "father of physics" because of his careful experimentation, he is shown here performing experiments by rolling balls on an inclined plane. He is perhaps best known for his experiments on motion, the development of the telescope, and his many astronomical discoveries. He came into disfavor with the Catholic Church for his belief in the Copernican theory. He was finally cleared of heresy by Pope John Paul II in 1992, 350 years after his death.

Newton's laws

Isaac Newton (1642–1727), the great English physicist and mathematician, did most of his work at Cambridge where he was educated and became the Lucasian Professor of Mathematics. He was known not only for his work on the laws of motion but also as a founder of optics. His useful works are too numerous to list here, but it should be mentioned that he spent a considerable amount of his time on alchemy, theology, and the spiritual universe. His writings on these subjects, which were dear to him, were quite unorthodox. This painting shows him performing experiments with light.

**Maxwell's equations** 

carefully the relationship between net force and acceleration, and his concepts were stated in three laws that bear his name today:

**Newton's first law:** An object in motion with a constant velocity will continue in motion unless acted upon by some net external force. A body at rest is just a special case of Newton's first law with zero velocity. Newton's first law is often called the *law of inertia* and is also used to describe inertial reference frames.

**Newton's second law:** The acceleration  $\vec{a}$  of a body is proportional to the net external force  $\vec{F}$  and inversely proportional to the mass m of the body. It is stated mathematically as

$$\vec{F} = m\vec{a} \tag{1.1a}$$

A more general statement\* relates force to the time rate of change of the linear momentum  $\vec{p}$ .

$$\vec{F} = \frac{d\vec{p}}{dt} \tag{1.1b}$$

**Newton's third law:** The force exerted by body 1 on body 2 is equal in magnitude and opposite in direction to the force that body 2 exerts on body 1. If the force on body 2 by body 1 is denoted by  $\vec{F}_{21}$ , then Newton's third law is written as

$$\vec{F}_{21} = -\vec{F}_{12} \tag{1.2}$$

It is often called the law of action and reaction.

These three laws develop the concept of force. Using that concept together with the concepts of velocity  $\vec{v}$ , acceleration  $\vec{a}$ , linear momentum  $\vec{p}$ , rotation (angular velocity  $\vec{\omega}$  and angular acceleration  $\vec{a}$ ), and angular momentum  $\vec{L}$ , we can describe the complex motion of bodies.

#### **Electromagnetism**

Electromagnetism developed over a long period of time. Important contributions were made by Charles Coulomb (1736–1806), Hans Christian Oersted (1777–1851), Thomas Young (1773–1829), André Ampère (1775–1836), Michael Faraday (1791–1867), Joseph Henry (1797–1878), James Clerk Maxwell (1831–1879), and Heinrich Hertz (1857–1894). Maxwell showed that electricity and magnetism were intimately connected and were related by a change in the inertial frame of reference. His work also led to the understanding of electromagnetic radiation, of which light and optics are special cases. Maxwell's four equations, together with the Lorentz force law, explain much of electromagnetism.

Gauss's law for electricity  $\oint_{c} \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$  (1.3)

Gauss's law for magnetism 
$$\oint \vec{B} \cdot d\vec{A} = 0$$
 (1.4)

$$\oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt} \tag{1.5}$$

<sup>\*</sup>It is a remarkable fact that Newton wrote his second law not as  $\vec{F} = m\vec{a}$ , but as  $\vec{F} = d(m\vec{v})/dt$ , thus taking into account mass flow and change in velocity. This has applications in both fluid mechanics and rocket propulsion.

Generalized Ampere's law 
$$\oint \vec{B} \cdot d\vec{s} = \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} + \mu_0 I$$
 (1.6)

Lorentz force law 
$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$
 (1.7)

Maxwell's equations indicate that charges and currents create fields, and in turn, these fields can create other fields, both electric and magnetic.

#### Thermodynamics

Thermodynamics deals with temperature T, heat Q, work W, and the internal energy of systems U. The understanding of the concepts used in thermodynamics such as pressure P, volume V, temperature, thermal equilibrium, heat, entropy, and especially energy—was slow in coming. We can understand the concepts of pressure and volume as mechanical properties, but the concept of temperature must be carefully considered. We have learned that the internal energy of a system of noninteracting point masses depends only on the temperature.

Important contributions to thermodynamics were made by Benjamin Thompson (Count Rumford, 1753–1814), Sadi Carnot (1796–1832), James Joule (1818–1889), Rudolf Clausius (1822–1888), and William Thomson (Lord Kelvin, 1824–1907). The primary results of thermodynamics can be described in two laws:

**First law of thermodynamics:** The change in the internal energy  $\Delta U$  of a system is equal **Laws of thermodynamics** to the heat Q added to the system plus the work W done on the system.

$$\Delta U = Q + W \tag{1.8}$$

The first law of thermodynamics generalizes the conservation of energy by including heat.

Second law of thermodynamics: It is not possible to convert heat completely into work without some other change taking place. Various forms of the second law state similar, but slightly different, results. For example, it is not possible to build a perfect engine or a perfect refrigerator. It is not possible to build a perpetual motion machine. Heat does not spontaneously flow from a colder body to a hotter body without some other change taking place. The second law forbids all these from happening. The first law states the conservation of energy, but the second law says what kinds of energy processes cannot take place. For example, it is possible to completely convert work into heat, but not vice versa, without some other change taking place.

Two other "laws" of thermodynamics are sometimes expressed. One is called the "zeroth" law, and it is useful in understanding temperature. It states that *if two* thermal systems are in thermodynamic equilibrium with a third system, they are in equilibrium with each other. We can state it more simply by saying that two systems at the same temperature as a third system have the same temperature as each other. This concept was not explicitly stated until the twentieth century. The "third" law of thermodynamics expresses that it is not possible to achieve an absolute zero temperature.

#### The Kinetic Theory of Gases 1.2

We understand now that gases are composed of atoms and molecules in rapid motion, bouncing off each other and the walls, but in the 1890s this had just gained acceptance. The kinetic theory of gases is related to thermodynamics and

to the atomic theory of matter, which we discuss in Section 1.5. Experiments were relatively easy to perform on gases, and the Irish chemist Robert Boyle (1627–1691) showed around 1662 that the pressure times the volume of a gas was constant for a constant temperature. The relation PV = constant (for constant T) is now referred to as *Boyle's law*. The French physicist Jacques Charles (1746–1823) found that V/T = constant (at constant pressure), referred to as *Charles's law*. Joseph Louis Gay-Lussac (1778–1850) later produced the same result, and the law is sometimes associated with his name. If we combine these two laws, we obtain the ideal gas equation

**Ideal gas equation** 

$$PV = nRT \tag{1.9}$$

where *n* is the number of moles and *R* is the ideal gas constant, 8.31 J/mol  $\cdot$  K.

1

In 1811 the Italian physicist Amedeo Avogadro (1776–1856) proposed that equal volumes of gases at the same temperature and pressure contained equal numbers of molecules. This hypothesis was so far ahead of its time that it was not accepted for many years. The famous English chemist John Dalton opposed the idea because he apparently misunderstood the difference between atoms and molecules. Considering the rudimentary nature of the atomic theory of matter at the time, this was not surprising.

Daniel Bernoulli (1700–1782) apparently originated the kinetic theory of gases in 1738, but his results were generally ignored. Many scientists, including Newton, Laplace, Davy, Herapath, and Waterston, had contributed to the development of kinetic theory by 1850. Theoretical calculations were being compared with experiments, and by 1895 the kinetic theory of gases was widely accepted. The statistical interpretation of thermodynamics was made in the latter half of the nineteenth century by Maxwell, the Austrian physicist Ludwig Boltzmann (1844–1906), and the American physicist J. Willard Gibbs (1839–1903).

In introductory physics classes, the kinetic theory of gases is usually taught by applying Newton's laws to the collisions that a molecule makes with other molecules and with the walls. A representation of a few molecules colliding is shown in Figure 1.1. In the simple model of an ideal gas, only elastic collisions are considered. By taking averages over the collisions of many molecules, the ideal gas law, Equation (1.9), is revealed. The average kinetic energy of the molecules is shown to be linearly proportional to the temperature, and the internal energy U is

$$U = nN_{\rm A}\langle K \rangle = \frac{3}{2} nRT \tag{1.10}$$

where *n* is the number of moles of gas,  $N_A$  is Avogadro's number,  $\langle K \rangle$  is the average kinetic energy of a molecule, and *R* is the ideal gas constant. This relation ignores any nontranslational contributions to the molecular energy, such as rotations and vibrations.

However, energy is not represented only by translational motion. It became clear that all *degrees of freedom*, including rotational and vibrational, were also capable of carrying energy. The *equipartition theorem* states that each degree of freedom of a molecule has an average energy of kT/2, where k is the Boltzmann constant ( $k = R/N_A$ ). Translational motion has three degrees of freedom, and rotational and vibrational modes can also be excited at higher temperatures. If there are f degrees of freedom, then Equation (1.10) becomes

**Internal energy** 



Figure 1.1 Molecules inside a closed container are shown colliding with the walls and with each other. The motions of a few molecules are indicated by the arrows. The number of molecules inside the container is huge.

#### Statistical thermodynamics

**Equipartition theorem** 

 $U = \frac{f}{2} nRT \tag{1.11}$ 

The molar (n = 1) heat capacity  $c_V$  at constant volume for an ideal gas is the rate of change in internal energy with respect to change in temperature and is given by

$$c_{\rm V} = \frac{3}{2}R \tag{1.12}$$
 Heat capacity

The experimental quantity  $c_V/R$  is plotted versus temperature for hydrogen in Figure 1.2. The ratio  $c_V/R$  is equal to 3/2 for low temperatures, where only translational kinetic energy is important, but it rises to 5/2 at 300 K, where rotations occur for H<sub>2</sub>, and finally reaches 7/2, because of vibrations at still higher temperatures, before the molecule dissociates. Although the kinetic theory of gases fails to predict specific heats for real gases, it leads to models that can be used on a gas-by-gas basis. Kinetic theory is also able to provide useful information on other properties such as diffusion, speed of sound, mean free path, and collision frequency.

In the 1850s Maxwell derived a relation for the distribution of speeds of the molecules in gases. The distribution of speeds f(v) is given as a function of the speed and the temperature by the equation

$$f(v) = 4\pi N \left(\frac{m}{2\pi kT}\right)^{3/2} v^2 e^{-mv^2/2kT}$$
(1.13) Maxwell's speed  
(1.13) distribution

where *m* is the mass of a molecule and *T* is the temperature. This result is plotted for nitrogen in Figure 1.3 for temperatures of 300 K, 1000 K, and 4000 K. The peak of each distribution is the most probable speed of a gas molecule for the given temperature. In 1895 measurement was not precise enough to confirm Maxwell's distribution, and it was not confirmed experimentally until 1921.

By 1895 Boltzmann had made Maxwell's calculation more rigorous, and the general relation is called the *Maxwell-Boltzmann distribution*. The distribution can be used to find the *root-mean-square* speed  $v_{\rm rms}$ ,

$$v_{\rm rms} = \sqrt{\langle v^2 \rangle} = \sqrt{\frac{3kT}{m}} \tag{1.14}$$

which shows the relationship of the energy to the temperature for an ideal gas:

$$U = nN_{\rm A}\langle K \rangle = nN_{\rm A}\frac{m\langle v^2 \rangle}{2} = nN_{\rm A}\frac{m3kT}{2m} = \frac{3}{2}nRT \qquad (1.15)$$

This was the result of Equation (1.10).



**Figure 1.2** The molar heat capacity at constant volume  $(c_V)$  divided by R ( $c_V/R$  is dimensionless) is displayed as a function of temperature for hydrogen gas. Note that as the temperature increases, the rotational and vibrational modes become important. This experimental result is consistent with the equipartition theorem, which adds kT/2 of energy per molecule (RT/2 per mole) for each degree of freedom.





#### 1.3 Waves and Particles

We first learned the concepts of velocity, acceleration, force, momentum, and energy in introductory physics by using a single particle with its mass concentrated in one small point. In order to adequately describe nature, we add twoand three-dimensional bodies and rotations and vibrations. However, many aspects of physics can still be treated as if the bodies are simple particles. In particular, the kinetic energy of a moving particle is one way that energy can be transported from one place to another.

But we have found that many natural phenomena can be explained only in terms of *waves*, which are traveling disturbances that carry energy. This description includes standing waves, which are superpositions of traveling waves. Most waves, like water waves and sound waves, need an elastic medium in which to move. Curiously enough, matter is not transported in waves—but energy is. Mass may oscillate, but it doesn't actually propagate along with the wave. Two examples are a cork and a boat on water. As a water wave passes, the cork gains energy as it moves up and down, and after the wave passes, the cork remains. The boat also reacts to the wave, but it primarily rocks back and forth, throwing around things that are not fixed on the boat. The boat obtains considerable kinetic energy from the wave. After the wave passes, the boat eventually returns to rest.

Waves and particles were the subject of disagreement as early as the seventeenth century, when there were two competing theories of the nature of light. Newton supported the idea that light consisted of corpuscles (or particles). He performed extensive experiments on light for many years and finally published his book *Opticks* in 1704. *Geometrical optics* uses straight-line, particle-like trajectories called rays to explain familiar phenomena such as reflection and refraction. Geometrical optics was also able to explain the apparent observation of sharp shadows. The competing theory considered light as a wave phenomenon. Its strongest proponent was the Dutch physicist Christian Huygens (1629–1695), who presented his theory in 1678. The wave theory could also explain reflection and refraction, but it could not explain the sharp shadows observed. Experimental physics of the 1600s and 1700s was not able to discern between the two competing theories. Huygens's poor health and other duties kept him from working on optics much after 1678. Although Newton did not feel strongly about his corpuscular

#### **Energy transport**

#### Nature of light: waves or particles?

theory, the magnitude of his reputation caused it to be almost universally accepted for more than a hundred years and throughout most of the eighteenth century.

Finally, in 1802, the English physician Thomas Young (1773–1829) announced the results of his two-slit interference experiment, indicating that light behaved as a wave. Even after this singular event, the corpuscular theory had its supporters. During the next few years Young and, independently, Augustin Fresnel (1788–1827) performed several experiments that clearly showed that light behaved as a wave. By 1830 most physicists believed in the wave theory—some 150 years after Newton performed his first experiments on light.

One final experiment indicated that the corpuscular theory was difficult to accept. Let c be the speed of light in vacuum and v be the speed of light in another medium. If light behaves as a particle, then to explain refraction, light must speed up when going through denser material (v > c). The wave theory of Huygens predicts just the opposite (v < c). The measurements of the speed of light in various media were slowly improving, and finally, in 1850, Foucault showed that *light traveled more slowly in water than in air*. The corpuscular theory seemed incorrect. Newton would probably have been surprised that his weakly held beliefs lasted as long as they did. Now we realize that geometrical optics is correct only if the wavelength of light is much smaller than the size of the obstacles and apertures that the light encounters.

Figure 1.4 shows the "shadows" or *diffraction patterns* from light falling on sharp edges. In Figure 1.4a the alternating black and white lines can be seen all around the razor blade's edges. Figure 1.4b is a highly magnified photo of the diffraction from a sharp edge. The bright and dark regions can be understood only if light is a wave and not a particle. The physicists of 200 to 300 years ago apparently did not observe such phenomena. They believed that shadows were sharp, and only the particle nature of light could explain their observations.

In the 1860s Maxwell showed that electromagnetic waves consist of oscillating electric and magnetic fields. Visible light covers just a narrow range of the total electromagnetic spectrum, and all electromagnetic radiation travels at the speed of light c in free space, given by

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = \lambda f \tag{1.16}$$

where  $\lambda$  is the wavelength and *f* is the frequency. The fundamental constants  $\mu_0$  and  $\epsilon_0$  are defined in electricity and magnetism and reveal the connection to the speed of light. In 1887 the German physicist Heinrich Hertz (1857–1894) succeeded in generating and detecting electromagnetic waves having wavelengths



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(b)
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far outside the visible range ( $\lambda \approx 5$  m). The properties of these waves were just as Maxwell had predicted. His results continue to have far-reaching effects in modern telecommunications: cable TV, cell phones, lasers, fiber optics, wireless Internet, and so on.

Some unresolved issues about electromagnetic waves in the 1890s eventually led to one of the two great modern theories, the *theory of relativity* (see Section 1.6 and Chapter 2). Waves play a central and essential role in the other great modern physics theory, *quantum mechanics*, which is sometimes called *wave mechanics*. Because waves play such a central role in modern physics, we review their properties in Chapter 5.

# 1.4 Conservation Laws and Fundamental Forces

Conservation laws are the guiding principles of physics. The application of a few laws explains a vast quantity of physical phenomena. We listed the conservation laws of classical physics in Section 1.1. They include energy, linear momentum, angular momentum, and charge. Each of these is extremely useful in introductory physics. We use linear momentum when studying collisions, and the conservation laws when examining dynamics. We have seen the concept of the conservation of energy change. At first we had only the conservation of kinetic energy in a force-free region. Then we added potential energy and formed the conservation of mechanical energy. In our study of thermodynamics, we added internal energy, and so on. The study of electrical circuits was made easier by the conservation of charge flow at each junction and the conservation of energy throughout all the circuit elements.

Much of what we know about conservation laws and fundamental forces has been learned within the last hundred years. In our study of modern physics we will find that mass is added to the conservation of energy, and the result is sometimes called the *conservation of mass-energy*, although the term *conservation of energy* is still sufficient and generally used. When we study elementary particles we will add the conservation of baryons and the conservation of leptons. Closely related to conservation laws are invariance principles. Some parameters are invariant in some interactions or in specific systems but not in others. Examples include time reversal, parity, and distance. We will study the Newtonian or Galilean invariance and find it lacking in our study of relativity; a new invariance principle will be needed. In our study of nuclear and elementary particles, conservation laws and invariance principles will often be used (see Figure 1.5).

#### **Fundamental Forces**

In introductory physics, we often begin our study of forces by examining the reaction of a mass at the end of a spring, because the spring force can be easily calibrated. We subsequently learn about tension, friction, gravity, surface, electrical, and magnetic forces. Despite the seemingly complex array of forces, we presently believe there are only three fundamental forces. All the other forces can be derived from them. These three forces are the **gravitational**, **electroweak**, and **strong** forces. Some physicists refer to the electroweak interaction as separate electromagnetic and weak forces because the unification occurs only at very high energies. The approximate strengths and ranges of the three fundamental forces are listed in Table 1.1. Physicists sometimes use the term *interaction* when



**Figure 1.5** The conservation laws of momentum and energy are invaluable in untangling complex particle reactions like the one shown here, where a 5-GeV  $K^-$  meson interacts with a proton at rest to produce an  $\Omega^-$  in a bubble chamber. The uncharged  $K^0$  is not observed. Notice the curved paths of the charged particles in the magnetic field. Such reactions are explained in Chapter 14.

Interaction		Relative Strength*	Range
Strong		1	Short, $\sim 10^{-15}$ m
Electroweak	Electromagnetic	$10^{-2}$	Long, $1/r^2$
	∫ Weak	$10^{-9}$	Short, $\sim 10^{-15}$ m
Gravitational		$10^{-39}$	Long, $1/r^2$

referring to the fundamental forces because it is the overall interaction among the constituents of a system that is of interest.

The gravitational force is the weakest. It is the force of mutual attraction between masses and, according to Newton, is given by

$$\vec{F}_g = -G \frac{m_1 m_2}{r^2} \hat{r}$$
(1.17) Gravitation

where  $m_1$  and  $m_2$  are two point masses, G is the gravitational constant, r is the distance between the masses, and  $\hat{r}$  is a unit vector directed along the line between the two point masses (attractive force). The gravitational force is noticeably effective only on a macroscopic scale, but it has tremendous importance: it is the force that keeps Earth rotating about our source of life energy-the sunand that keeps us and our atmosphere anchored to the ground. Gravity is a long-range force that diminishes as  $1/r^2$ .

The primary component of the electroweak force is *electromagnetic*. The other component is the weak interaction, which is responsible for beta decay in nuclei, among other processes. In the 1970s Sheldon Glashow, Steven Weinberg, and Abdus Salam predicted that the electromagnetic and weak forces were in fact facets of the same force. Their theory predicted the existence of new particles, called Wand Z bosons, which were discovered in 1983. We discuss bosons and the experiment in Chapter 14. For all practical purposes, the weak interaction is effective in the nucleus only over distances the size of  $10^{-15}$  m. Except when dealing with very high energies, physicists mostly treat nature as if the electromagnetic and weak forces were separate. Therefore, you will sometimes see references to the *four* fundamental forces (gravity, strong, electromagnetic, and weak).

The electromagnetic force is responsible for holding atoms together, for friction, for contact forces, for tension, and for electrical and optical signals. It is responsible for all chemical and biological processes, including cellular structure and nerve processes. The list is long because the electromagnetic force is responsible for practically all nongravitational forces that we experience. The electrostatic, or Coulomb, force between two point charges  $q_1$  and  $q_2$ , separated by a distance r, is given by

$$ec{F}_C = rac{1}{4\pi\epsilon_0} rac{q_1q_2}{r^2}\,\hat{r}$$

The easiest way to remember the vector direction is that like charges repel and unlike charges attract. Moving charges also create and react to magnetic fields [see Equation (1.7)].

#### al interaction

#### Weak interaction

#### **Electromagnetic** interaction

#### **Coulomb force** (1.18)

**Strong interaction** The third fundamental force, the strong force, is the one holding the nucleus together. It is the strongest of all the forces, but it is effective only over short distances—on the order of  $10^{-15}$  m. The strong force is so strong that it easily binds two protons inside a nucleus even though the electrical force of repulsion over the tiny confined space is huge. The strong force is able to contain dozens of protons inside the nucleus before the electrical force of repulsion becomes strong enough to cause nuclear decay. We study the strong force extensively in this book, learning that neutrons and protons are composed of *quarks*, and that the part of the strong force acting between quarks has the unusual name of *color* force.

Physicists strive to combine forces into more fundamental ones. Centuries ago the forces responsible for friction, contact, and tension were all believed to be different. Today we know they are all part of the electroweak force. Two hundred years ago scientists thought the electrical and magnetic forces were independent, but after a series of experiments, physicists slowly began to see their connection. This culminated in the 1860s in Maxwell's work, which clearly showed they were but part of one force and at the same time explained light and other radiation. Figure 1.6 is a diagram of the unification of forces over time. Newton certainly had an inspiration when he was able to unify the planetary motions with the apple falling from the tree. We will see in Chapter 15 that Einstein was even able to link gravity with space and time.

The further unification of forces currently remains one of the most active research fields. Considerable efforts have been made to unify the electroweak and strong forces through the *grand unified theories*, or GUTs. A leading GUT is the mathematically complex *string theory*. Several predictions of these theories have not yet been verified experimentally (for example, the instability of the proton and the existence of magnetic monopoles). We present some of the exciting research areas in present-day physics throughout this book, because these



**Unification of forces** 

Figure 1.6 The three fundamental forces (shown in the heavy boxes) are themselves unifications of forces that were once believed to be fundamental. Present research is under way (see blue lines) to further unify the fundamental forces into a single force. topics are the ones you will someday read about on the front pages of newspapers and in the weekly news magazines and perhaps will contribute to in your own careers.

# **1.5** The Atomic Theory of Matter

Today the idea that matter is composed of tiny particles called *atoms* is taught in elementary school and expounded throughout later schooling. We are told that the Greek philosophers Democritus and Leucippus proposed the concept of atoms as early as 450 B.C. The smallest piece of matter, which could not be subdivided further, was called an *atom*, after the Greek word *atomos*, meaning "indivisible." Physicists do not discredit the early Greek philosophers for thinking that the basic entity of life consisted of atoms. For centuries, scientists were called "natural philosophers," and in this tradition the highest university degree American scientists receive is a Ph.D., which stands for doctor of philosophy.

Not many new ideas were proposed about atoms until the seventeenth century, when scientists started trying to understand the properties and laws of gases. The work of Boyle, Charles, and Gay-Lussac presupposed the interactions of tiny particles in gases. Chemists and physical chemists made many important advances. In 1799 the French chemist Proust (1754–1826) proposed the *law of definite proportions*, which states that when two or more elements combine to form a compound, the proportions by weight (or mass) of the elements are always the same. Water (H<sub>2</sub>O) is always formed of one part hydrogen and eight parts oxygen by mass.

The English chemist John Dalton (1766–1844) is given most of the credit for originating the modern atomic theory of matter. In 1803 he proposed that the atomic theory of matter could explain the law of definite proportions if the elements are composed of atoms. Each element has atoms that are physically and chemically characteristic. The concept of atomic weights (or masses) was the key to the atomic theory.

In 1811 the Italian physicist Avogadro proposed the existence of molecules, consisting of individual or combined atoms. He stated without proof that *all gases contain the same number of molecules in equal volumes at the same temperature and pressure.* Avogadro's ideas were ridiculed by Dalton and others who could not imagine that atoms of the same element could combine. If this could happen, they argued, then all the atoms of a gas would combine to form a liquid. The concept of molecules and atoms was indeed difficult to imagine, but finally, in 1858, the Italian chemist Cannizzaro (1826–1910) solved the problem and showed how Avogadro's ideas could be used to find atomic masses. Today we think of an atom as the smallest unit of matter that can be identified with a particular element. A molecule can be a single atom or a combination of two or more atoms of either like or dissimilar elements. Molecules can consist of thousands of atoms.

The number of molecules in one gram-molecular weight of a particular element (6.023 × 10<sup>23</sup> molecules/mol) is called Avogadro's number ( $N_A$ ). For example, one mole of hydrogen (H<sub>2</sub>) has a mass of about 2 g and one mole of carbon has a mass of about 12 g; one mole of each substance consists of 6.023 × 10<sup>23</sup> atoms. Avogadro's number was not even estimated until 1865, and it was finally accurately measured by Perrin, as we discuss at the end of this section.

During the mid-1800s the kinetic theory of gases was being developed, and because it was based on the concept of atoms, its successes gave validity to the

#### Dalton, the father of the atomic theory

#### Avogadro's number

atomic theory. The experimental results of specific heats, Maxwell speed distribution, and transport phenomena (see the discussion in Section 1.2) all supported the concept of the atomic theory.

In 1827 the English botanist Robert Brown (1773–1858) observed with a microscope the motion of tiny pollen grains suspended in water. The pollen appeared to dance around in random motion, while the water was still. At first the motion (now called *Brownian motion*) was ascribed to convection or organic matter, but eventually it was observed to occur for any tiny particle suspended in liquid. The explanation according to the atomic theory is that the molecules in the liquid are constantly bombarding the tiny grains. A satisfactory explanation was not given until the twentieth century (by Einstein).

Although it may appear, according to the preceding discussion, that the atomic theory of matter was universally accepted by the end of the nineteenth century, that was not the case. Certainly most physicists believed in it, but there was still opposition. A principal leader in the antiatomic movement was the renowned Austrian physicist Ernst Mach. Mach was an absolute positivist, believing in the reality of nothing but our own sensations. A simplified version of his line of reasoning would be that because we have never *seen* an atom, we cannot say anything about its reality. The Nobel Prize–winning German physical chemist Wilhelm Ostwald supported Mach philosophically but also had more practical arguments on his side. In 1900 there were difficulties in understanding radioactivity, x rays, discrete spectral lines, and how atoms formed molecules and solids. Ostwald contended that we should therefore think of atoms as hypothetical constructs, useful for bookkeeping in chemical reactions.

On the other hand, there were many believers in the atomic theory. Max Planck, the originator of quantum theory, grudgingly accepted the atomic theory of matter because his radiation law supported the existence of submicroscopic quanta. Boltzmann was convinced that atoms must exist, mainly because they were necessary in his statistical mechanics. It is said that Boltzmann committed suicide in 1905 partly because he was despondent that so many people rejected his theory. Today we have pictures of the atom (see Figure 1.7) that would



Figure 1.7 This scanning tunneling microscope photo, called the "stadium corral," shows 76 individually placed iron atoms on a copper surface. The IBM researchers were trying to contain and modify electron density, observed by the wave patterns, by surrounding the electrons inside the quantum "corral." Researchers are thus able to study the quantum behavior of electrons. See also the Special Topic on Scanning Probe Microscopes in Chapter 6.

Opposition to atomic theory

undoubtedly have convinced even Mach, who died in 1916 still unconvinced of the validity of the atomic theory.

Overwhelming evidence for the existence of atoms was finally presented in the first decade of the twentieth century. First, Einstein, in one of his three famous papers published in 1905 (the others were about special relativity and the photoelectric effect), provided an explanation of the Brownian motion observed almost 80 years earlier by Robert Brown. Einstein explained the motion in terms of molecular motion and presented theoretical calculations for the *random walk* problem. A random walk (often called the *drunkard's walk*) is a statistical process that determines how far from its initial position a tiny grain may be after many random molecular collisions. Einstein was able to determine the approximate masses and sizes of atoms and molecules from experimental data.

Finally, in 1908, the French physicist Jean Perrin (1870–1942) presented data from an experiment designed using kinetic theory that agreed with Einstein's predictions. Perrin's experimental method of observing many particles of different sizes is a classic work, for which he received the Nobel Prize for Physics in 1926. His experiment utilized four types of measurements. Each was consistent with the atomic theory, and each gave a quantitative determination of Avogadro's number—the first accurate measurements that had been made. Since 1908 the atomic theory of matter has been accepted by practically everyone.

# 1.6 Unresolved Questions of 1895 and New Horizons

We choose 1895 as a convenient time to separate the periods of classical and modern physics, although this is an arbitrary choice based on discoveries made in 1895–1897. The thousand or so physicists living in 1895 were rightfully proud of the status of their profession. The precise experimental method was firmly established. Theories were available that could explain many observed phenomena. In large part, scientists were busy measuring and understanding such physical parameters as specific heats, densities, compressibility, resistivity, indices of refraction, and permeabilities. The pervasive feeling was that, given enough time, everything in nature could be understood by applying the careful thinking and experimental techniques of physics. The field of mechanics was in particularly good shape, and its application had led to the stunning successes of the kinetic theory of gases and statistical thermodynamics.

In hindsight we can see now that this euphoria of success applied only to the macroscopic world. Objects of human dimensions such as automobiles, steam engines, airplanes, telephones, and electric lights either existed or were soon to appear and were triumphs of science and technology. However, the atomic theory of matter was not universally accepted, and what made up an atom was purely conjecture. The structure of matter was unknown.

There were certainly problems that physicists could not resolve. Only a few of the deepest thinkers seemed to be concerned with them. Lord Kelvin, in a speech in 1900 to the Royal Institution, referred to "two clouds on the horizon." These were the electromagnetic medium and the failure of classical physics to explain blackbody radiation. We mention these and other problems here. Their solutions were soon to lead to two of the greatest breakthroughs in human thought ever recorded—the theories of quantum physics and of relativity.

# Overwhelming evidence of atomic theory

#### **Experiment and reasoning**

#### **Clouds on the horizon**



William Thomson (Lord Kelvin, 1824–1907) was born in Belfast, Ireland, and at age 10 entered the University of Glasgow in Scotland where his father was a professor of mathematics. He graduated from the University of Cambridge and, at age 22, accepted the chair of natural philosophy (later called physics) at the University of Glasgow, where he finished his illustrious 53-year career, finally resigning in 1899 at age 75. Lord Kelvin's contributions to nineteenth-century science were far reaching, and he made contributions in electricity, magnetism, thermodynamics, hydrodynamics, and geophysics. He was involved in the successful laying of the transatlantic cable. He was arguably the preeminent scientist of the latter part of the nineteenth century. He was particularly well known for his prediction of the Earth's age, which would later turn out to be inaccurate (see Chapter 12).

> Ultraviolet catastrophe: infinite emissivity

**Electromagnetic Medium.** The waves that were well known and understood by physicists all had media in which the waves propagated. Water waves traveled in water, and sound waves traveled in any material. It was natural for nineteenth-century physicists to assume that electromagnetic waves also traveled in a medium, and this medium was called the *ether*. Several experiments, the most notable of which were done by Michelson, had sought to detect the ether without success. An extremely careful experiment by Michelson and Morley in 1887 was so sensitive, it should have revealed the effects of the ether. Subsequent experiments to check other possibilities were also negative. In 1895 some physicists were concerned that the elusive ether could not be detected. Was there an alternative explanation?

**Electrodynamics.** The other difficulty with Maxwell's electromagnetic theory had to do with the electric and magnetic fields as seen and felt by moving bodies. What appears as an electric field in one reference system may appear as a magnetic field in another system moving with respect to the first. Although the relationship between electric and magnetic fields seemed to be understood by using Maxwell's equations, the equations do not keep the same form under a Galilean transformation [see Equations (2.1) and (2.2)], a situation that concerned both Hertz and Lorentz. Hertz unfortunately died in 1894 at the young age of 36 and never experienced the modern physics revolution. The Dutch physicist Hendrik Lorentz (1853–1928), on the other hand, proposed a radical idea that solved the electrodynamics problem: space was contracted along the direction of motion of the body. George FitzGerald in Ireland independently proposed the same concept. The Lorentz-FitzGerald hypothesis, proposed in 1892, was a precursor to Einstein's theory advanced in 1905 (see Chapter 2).

**Blackbody Radiation.** In 1895 thermodynamics was on a strong footing; it had achieved much success. One of the interesting experiments in thermodynamics concerns an object, called a *blackbody*, that absorbs the entire spectrum of electromagnetic radiation incident on it. An enclosure with a small hole serves as a blackbody, because all the radiation entering the hole is absorbed. A blackbody also emits radiation, and the emission spectrum shows the electromagnetic power emitted per unit area. The radiation emitted covers all frequencies, each with its own intensity. Precise measurements were carried out to determine the spectrum of blackbody radiation, such as that shown in Figure 1.8. Blackbody radiation was a fundamental issue, because the emission spectrum is independent of the body itself—it is characteristic of all blackbodies.

Many physicists of the period—including Kirchhoff, Stefan, Boltzmann, Rubens, Pringsheim, Lummer, Wien, Lord Rayleigh, Jeans, and Planck—had worked on the problem. It was possible to understand the spectrum both at the low-frequency end and at the high-frequency end, but no single theory could account for the entire spectrum. When the most modern theory of the day (the equipartition of energy applied to standing waves in a cavity) was applied to the problem, the result led to an *infinite* emissivity (or energy density) for high frequencies. The failure of the theory was known as the "ultraviolet catastrophe." The solution of the problem by Max Planck in 1900 would shake the very foundations of physics.



**Figure 1.8** The blackbody spectrum, showing the emission spectrum of radiation emitted from a blackbody as a function of the radiation wavelength. Different curves are produced for different temperatures, but they are independent of the type of blackbody cavity. The intensity peaks at  $\lambda_{max}$ .

## **On the Horizon**

During the years 1895–1897 there were four discoveries that were all going to require deeper understanding of the atom. The first was the discovery of x rays by the German physicist Wilhelm Röntgen (1845–1923) in November 1895. Next came the accidental discovery of radioactivity by the French physicist Henri Becquerel (1852–1908), who in February 1896 placed uranium salt next to a carefully wrapped photographic plate. When the plate was developed, a silhouette of the uranium salt was evident—indicating the presence of a very penetrating ray.

The third discovery, that of the electron, was actually the work of several physicists over a period of years. Michael Faraday, as early as 1833, observed a gas discharge glow—evidence of electrons. Over the next few years, several scientists detected evidence of particles, called *cathode rays*, being emitted from charged cathodes. In 1896 Perrin proved that cathode rays were negatively charged. The discovery of the electron, however, is generally credited to the British physicist J. J. Thomson (1856–1940), who in 1897 isolated the electron (cathode ray) and measured its velocity and its ratio of charge to mass.

The final important discovery of the period was made by the Dutch physicist Pieter Zeeman (1865–1943), who in 1896 found that a single spectral line was sometimes separated into two or three lines when the sample was placed in a magnetic field. The (normal) *Zeeman effect* was quickly explained by Lorentz as the result of light being emitted by the motion of electrons inside the atom. Zeeman and Lorentz showed that the frequency of the light was affected by the magnetic field according to the classical laws of electromagnetism.

The unresolved issues of 1895 and the important discoveries of 1895–1897 bring us to the subject of this book, *Modern Physics*. In 1900 Max Planck completed his radiation law, which solved the blackbody problem but required that energy be quantized. In 1905 Einstein presented his three important papers on Brownian motion, the photoelectric effect, and special relativity. While the work of Planck and Einstein may have solved the problems of the nineteenth-century physicists, they broadened the horizons of physics and have kept physicists active ever since.



#### Summary

Physicists of the 1890s felt that almost anything in nature could be explained by the application of careful experimental methods and intellectual thought. The application of mechanics to the kinetic theory of gases and statistical thermodynamics, for example, was a great success.

The particle viewpoint of light had prevailed for over a hundred years, mostly because of the weakly held belief of the great Newton, but in the early 1800s the nature of light was resolved in favor of waves. In the 1860s Maxwell showed that his electromagnetic theory predicted a much wider frequency range of electromagnetic radiation than the visible optical phenomena. In the twentieth century, the question of waves versus particles was to reappear.

The conservation laws of energy, momentum, angular momentum, and charge are well established. The three fundamental forces are gravitational, electroweak, and strong. Over the years many forces have been unified into these three. Physicists are actively pursuing attempts to unify these three forces into only two or even just one single fundamental force. The atomic theory of matter assumes atoms are the smallest unit of matter that is identified with a characteristic element. Molecules are composed of atoms, which can be from different elements. The kinetic theory of gases assumes the atomic theory is correct, and the development of the two theories proceeded together. The atomic theory of matter was not fully accepted until around 1910, by which time Einstein had explained Brownian motion and Perrin had published overwhelming experimental evidence.

The year 1895 saw several outstanding problems that seemed to worry only a few physicists. These problems included the inability to detect an electromagnetic medium, the difficulty in understanding the electrodynamics of moving bodies, and blackbody radiation. Four important discoveries during the period 1895–1897 were to signal the atomic age: x rays, radioactivity, the electron, and the splitting of spectral lines (Zeeman effect). The understanding of these problems and discoveries (among others) is the object of this book on modern physics.

# **Special Theory of Relativity**

It was found that there was no displacement of the interference fringes, so that the result of the experiment was negative and would, therefore, show that there is still a difficulty in the theory itself. . . .

Albert Michelson, Light Waves and Their Uses, 1907

One of the great theories of physics appeared early in the twentieth century when Albert Einstein presented his special theory of relativity in 1905. We learned in introductory physics that Newton's laws of motion must be measured relative to some reference frame. A reference frame is called an **inertial frame** if Newton's laws are valid in that frame. If a body subject to no net external force moves in a straight line with constant velocity, then the coordinate system attached to that body defines an inertial frame. If Newton's laws are valid in one reference frame, then they are also valid in a reference frame moving at a uniform velocity relative to the first system. This is known as the **Newtonian principle of relativity** or **Galilean invariance**.

Newton showed that it was not possible to determine absolute motion in space by any experiment, so he decided to use relative motion. In addition, the Newtonian concepts of time and space are completely separable. Consider two inertial reference frames, K and K', that move along their x and x' axes, respectively, with uniform relative velocity  $\vec{v}$  as shown in Figure 2.1. We show system K' moving to the right with velocity  $\vec{v}$  with respect to system K, which is fixed or



**Inertial frame** 

СНАРТЕК

#### **Galilean** invariance

**Figure 2.1** Two inertial systems are moving with relative speed v along their *x* axes. We show the system K at rest and the system K' moving with speed *v* relative to the system K.

stationary somewhere. One result of the relativity theory is that there are no fixed, absolute frames of reference. We use the term *fixed* to refer to a system that is fixed on a particular object, such as a planet, star, or spaceship that itself is moving in space. The transformation of the coordinates of a point in one system to the other system is given by

$$x' = x - vt$$
  

$$y' = y$$
  

$$z' = z$$
(2.1)

Similarly, the inverse transformation is given by

$$x = x' + vt$$
  

$$y = y'$$
  

$$z = z'$$
  
(2.2)

**Galilean transformation** 

where we have set t = t' because Newton considered time to be absolute. Equations (2.1) and (2.2) are known as the **Galilean transformation**. Newton's laws of motion are invariant under a Galilean transformation; that is, they have the same form in both systems K and K'.

In the late nineteenth century Albert Einstein was concerned that although Newton's laws of motion had the same form under a Galilean transformation, Maxwell's equations did not. Einstein believed so strongly in Maxwell's equations that he showed there was a significant problem in our understanding of the Newtonian principle of relativity. In 1905 he published ideas that rocked the very foundations of physics and science. He proposed that space and time are not separate and that Newton's laws are only an approximation. This special theory of relativity and its ramifications are the subject of this chapter. We begin by presenting the experimental situation historically—showing why a problem existed and what was done to try to rectify the situation. Then we discuss Einstein's two postulates on which the special theory is based. The interrelation of space and time is discussed, and several amazing and remarkable predictions based on the new theory are shown.

As the concepts of relativity became used more often in everyday research and development, it became essential to understand the transformation of momentum, force, and energy. Here we study relativistic dynamics and the relationship between mass and energy, which leads to one of the most famous equations in physics and a new conservation law of mass-energy. Finally, we return to electromagnetism to investigate the effects of relativity. We learn that Maxwell's equations don't require change, and electric and magnetic effects are relative, depending on the observer. We leave until Chapter 15 our discussion of Einstein's general theory of relativity.

# 2.1 The Apparent Need for Ether

Thomas Young, an English physicist and physician, performed his famous experiments on the interference of light in 1802. A decade later, the French physicist and engineer Augustin Fresnel published his calculations showing the detailed understanding of interference, diffraction, and polarization. Because all known waves (other than light) require a medium in which to propagate (water waves have water, sound waves have, for example, air, and so on), it was naturally assumed that light also required a medium, even though light was apparently able to travel in vacuum through outer space. This medium was called the *luminiferous ether* or just **ether** for short, and it must have some amazing properties. The ether had to have such a low density that planets could pass through it, seemingly for eternity, with no apparent loss of orbit position. Its elasticity must be strong enough to pass waves of incredibly high speeds!

The electromagnetic theory of light (1860s) of the Scottish mathematical physicist James Clerk Maxwell shows that the speed of light in different media depends only on the electric and magnetic properties of matter. In vacuum, the speed of light is given by  $v = c = 1/\sqrt{\mu_0\epsilon_0}$ , where  $\mu_0$  and  $\epsilon_0$  are the permeability and permittivity of free space, respectively. The properties of the ether, as proposed by Maxwell in 1873, must be consistent with electromagnetic theory, and the feeling was that to be able to discern the ether's various properties required only a sensitive enough experiment. The concept of ether was well accepted by 1880.

When Maxwell presented his electromagnetic theory, scientists were so confident in the laws of classical physics that they immediately pursued the aspects of Maxwell's theory that were in contradiction with those laws. As it turned out, this investigation led to a new, deeper understanding of nature. Maxwell's equations predict the velocity of light in a vacuum to be c. If we have a flashbulb go off in the moving system K', an observer in system K' measures the speed of the light pulse to be c. However, if we make use of Equation (2.1) to find the relation between speeds, we find the speed measured in system K to be c + v, where v is the relative speed of the two systems. However, Maxwell's equations don't differentiate between these two systems. Physicists of the late nineteenth century proposed that there must be one preferred inertial reference frame in which the ether was stationary and that in this system the speed of light was c. In the other systems, the speed of light would indeed be affected by the relative speed of the reference system. Because the speed of light was known to be so enormous,  $3 \times$  $10^8$  m/s, no experiment had as yet been able to discern an effect due to the relative speed v. The ether frame would in fact be an absolute standard, from which other measurements could be made. Scientists set out to find the effects of the ether.

# 2.2 The Michelson-Morley Experiment

The Earth orbits around the sun at a high orbital speed, about  $10^{-4}c$ , so an obvious experiment is to try to find the effects of the Earth's motion through the ether. Even though we don't know how fast the sun might be moving through the ether, the Earth's orbital *velocity* changes significantly throughout the year because of its change in direction, even if its orbital *speed* is nearly constant.

Albert Michelson (1852–1931) performed perhaps the most significant American physics experiment of the 1800s. Michelson, who was the first U.S. citizen to receive the Nobel Prize in Physics (1907), was an ingenious scientist who built an extremely precise device called an *interferometer*, which measures the phase difference between two light waves. Michelson used his interferometer to detect the difference in the speed of light passing through the ether in different directions. The basic technique is shown in Figure 2.2. Initially, it is assumed that one of the interferometer arms (AC) is parallel to the motion of the Earth through the ether. Light leaves the source S and passes through the glass plate at A. Because the back of A is partially silvered, part of the light is reflected,

#### The concept of ether



Albert A. Michelson (1852-1931) shown at his desk at the University of Chicago in 1927. He was born in Prussia but came to the United States when he was two years old. He was educated at the U.S. Naval Academy and later returned on the faculty. Michelson had appointments at several American universities including the Case School of Applied Science, Cleveland, in 1883; Clark University, Worcester, Massachusetts, in 1890; and the University of Chicago in 1892 until his retirement in 1929. During World War I he returned to the U.S. Navy, where he developed a rangefinder for ships. He spent his retirement years in Pasadena, California, where he continued to measure the speed of light at Mount Wilson.



eventually going to the mirror at D, and part of the light travels through A on to the mirror at C. The light is reflected at the mirrors C and D and comes back to the partially silvered mirror A, where part of the light from each path passes on to the telescope and eye at E. The compensator is added at B to make sure both light paths pass through equal thicknesses of glass. Interference fringes can be found by using a bright light source such as sodium, with the light filtered to make it monochromatic, and the apparatus is adjusted for maximum intensity of the light at E. We will show that the fringe pattern should shift if the apparatus is rotated through 90° such that arm AD becomes parallel to the motion of the Earth through the ether and arm AC is perpendicular to the motion.

We let the optical path lengths of AC and AD be denoted by  $\ell_1$  and  $\ell_2$ , respectively. The observed interference pattern consists of alternating bright and dark bands, corresponding to constructive and destructive interference, respectively (Figure 2.3). For constructive interference, the difference between the two



**Figure 2.2** A schematic diagram of Michelson's interferometer experiment. Light of a single wavelength is partially reflected and partially transmitted by the glass at A. The light is subsequently reflected by mirrors at C and D, and, after reflection or transmission again at A, enters the telescope at E. Interference fringes are visible to the observer at E.

**Figure 2.3** Interference fringes as they would appear in the eyepiece of the Michelson-Morley experiment.

path lengths (to and from the mirrors) is given by some number of wavelengths,  $2(\ell_1 - \ell_2) = n\lambda$ , where  $\lambda$  is the wavelength of the light and *n* is an integer.

The expected shift in the interference pattern can be calculated by determining the time difference between the two paths. When the light travels from A to C, the velocity of light according to the Galilean transformation is c + v, because the ether carries the light along with it. On the return journey from C to A the velocity is c - v, because the light travels opposite to the path of the ether. The total time for the round-trip journey to mirror M<sub>1</sub> is  $t_1$ :

$$t_1 = \frac{\ell_1}{c+v} + \frac{\ell_1}{c-v} = \frac{2c\ell_1}{c^2 - v^2} = \frac{2\ell_1}{c} \left(\frac{1}{1 - v^2/c^2}\right)$$

Now imagine what happens to the light that is reflected from mirror M<sub>2</sub>. If the light is pointed directly at point D, the ether will carry the light with it, and the light misses the mirror, much as the wind can affect the flight of an arrow. If a swimmer (who can swim with speed  $v_2$  in still water) wants to swim across a swiftly moving river (speed  $v_1$ ), the swimmer must start heading upriver, so that when the current carries her downstream, she will move directly across the river. Careful reasoning shows that the swimmer's velocity is  $\sqrt{v_2^2 - v_1^2}$  throughout her journey (Problem 4). Thus the time  $t_2$  for the light to pass to mirror M<sub>2</sub> at D and back is

$$t_2 = \frac{2\ell_2}{\sqrt{c^2 - v^2}} = \frac{2\ell_2}{c} \frac{1}{\sqrt{1 - v^2/c^2}}$$

The time difference between the two journeys  $\Delta t$  is

$$\Delta t = t_2 - t_1 = \frac{2}{c} \left( \frac{\ell_2}{\sqrt{1 - v^2/c^2}} - \frac{\ell_1}{1 - v^2/c^2} \right)$$
(2.3)

We now rotate the apparatus by 90° so that the ether passes along the length  $\ell_2$  toward the mirror M<sub>2</sub>. We denote the new quantities by primes and carry out an analysis similar to that just done. The time difference  $\Delta t'$  is now

$$\Delta t' = t'_2 - t'_1 = \frac{2}{c} \left( \frac{\ell_2}{1 - v^2/c^2} - \frac{\ell_1}{\sqrt{1 - v^2/c^2}} \right)$$
(2.4)

Michelson looked for a shift in the interference pattern when his apparatus was rotated by  $90^{\circ}$ . The time difference is

$$\Delta t' - \Delta t = \frac{2}{c} \left( \frac{\ell_1 + \ell_2}{1 - v^2 / c^2} - \frac{\ell_1 + \ell_2}{\sqrt{1 - v^2 / c^2}} \right)$$

Because we know  $c \gg v$ , we can use the binomial expansion\* to expand the terms involving  $v^2/c^2$ , keeping only the lowest terms.

$$\Delta t' - \Delta t = \frac{2}{c} (\ell_1 + \ell_2) \left[ \left( 1 + \frac{v^2}{c^2} + \cdots \right) - \left( 1 + \frac{v^2}{2c^2} + \cdots \right) \right]$$
$$\approx \frac{v^2 (\ell_1 + \ell_2)}{c^3}$$
(2.5)

Michelson left his position at the U.S. Naval Academy in 1880 and took his interferometer to Europe for postgraduate studies with some of Europe's best physi-

<sup>\*</sup>See Appendix 3 for the binomial expansion.



**Figure 2.4** An adaptation of the Michelson and Morley 1887 experiment taken from their publication [A. A. Michelson and E. M. Morley, *Philosophical Magazine* **190**, 449 (1887)]. (a) A perspective view of the apparatus. To reduce vibration, the experiment was done on a massive soapstone, 1.5 m square and 0.3 m thick. This stone was placed on a wooden float that rested on mercury inside the annular piece shown underneath the stone. The entire apparatus rested on a brick pier. (b) The incoming light is focused by the lens and is both transmitted and reflected by the partly silvered mirror. The adjustable mirror allows fine adjustments in the interference fringes. The stone was rotated slowly and uniformly on the mercury to look for the interference effects of the ether.

#### **Michelson in Europe**

cists, particularly Hermann Helmholtz in Berlin. After a few false starts he finally was able to perform a measurement in Potsdam (near Berlin) in 1881. In order to use Equation (2.5) for an estimate of the expected time difference, the value of the Earth's orbital speed around the sun,  $3 \times 10^4$  m/s, was used. Michelson's apparatus had  $\ell_1 \approx \ell_2 \approx \ell = 1.2$  m. Thus Equation (2.5) predicts a time difference of  $8 \times 10^{-17}$  s. This is an exceedingly small time, but for a visible wavelength of  $6 \times 10^{-7}$  m, the period of one wavelength amounts to  $T = 1/f = \lambda/c = 2 \times 10^{-15}$  s. Thus the time period of  $8 \times 10^{-17}$  s represents 0.04 fringes in the interference pattern. Michelson reasoned that he should be able to detect a shift of at least half this value but found none. Although disappointed, Michelson concluded that the hypothesis of the stationary ether must be incorrect.

The result of Michelson's experiment was so surprising that he was asked by several well-known physicists to repeat it. In 1882 Michelson accepted a position at the then-new Case School of Applied Science in Cleveland. Together with Edward Morley (1838–1923), a professor of chemistry at nearby Western Reserve College who had become interested in Michelson's work, he put together the more sophisticated experiment shown in Figure 2.4. The new experiment had an optical path length of 11 m, created by reflecting the light for eight round trips. The new apparatus was mounted on soapstone that floated on mercury to eliminate vibrations and was so effective that Michelson and Morley believed they could detect a fraction of a fringe shift as small as 0.005. With their new apparatus they expected the ether to produce a shift as large as 0.4 of a fringe. They reported in 1887 a *null result*—no effect whatsoever! The ether

Null result of Michelson-Morley experiment



**Figure 2.5** The effect of stellar aberration. (a) If a telescope is at rest, light from a distant star will pass directly into the telescope. (b) However, if the telescope is traveling at speed v (because it is fixed on the Earth, which has a motion about the sun), it must be slanted slightly to allow the starlight to enter the telescope. This leads to an apparent circular motion of the star as seen by the telescope, as the motion of the Earth about the sun changes throughout the solar year.

does not seem to exist. It is this famous experiment that has become known as the *Michelson-Morley experiment*.

The measurement so shattered a widely held belief that many suggestions were made to explain it. What if the Earth just happened to have a zero motion through the ether at the time of the experiment? Michelson and Morley repeated their experiment during night and day and for different seasons throughout the year. It is unlikely that at least sometime during these many experiments, the Earth would not be moving through the ether. Michelson and Morley even took their experiment to a mountaintop to see if the effects of the ether might be different. There was no change.

Of the many possible explanations of the null ether measurement, the one taken most seriously was the *ether drag* hypothesis. Some scientists proposed that the Earth somehow dragged the ether with it as the Earth rotates on its own axis and revolves around the sun. However, the ether drag hypothesis contradicts results from several experiments, including that of *stellar aberration* noted by the British astronomer James Bradley in 1728. Bradley noticed that the apparent position of the stars seems to rotate in a circular motion with a period of one year. The angular diameter of this circular motion with respect to the Earth is 41 seconds of arc. This effect can be understood by an analogy. From the viewpoint of a person sitting in a car during a rainstorm, the raindrops appear to fall vertically when the car is at rest but appear to be slanted toward the windshield when the car is moving forward. The same effect occurs for light coming from stars directly above the Earth's orbital plane. If the telescope and star are at rest with respect to the ether, the light enters the telescope as shown in Figure 2.5a. However, because the Earth is moving in its orbital motion, the apparent position of the star is at an angle  $\theta$  as shown in Figure 2.5b. The telescope must actually be slanted at an angle  $\theta$  to observe the light from the overhead star. During a time period t the starlight moves a vertical distance ct while the telescope moves a horizontal distance vt, so that the tangent of the angle  $\theta$  is

#### Ether drag

#### **Stellar aberration**

# $\tan \theta = \frac{vt}{ct} = \frac{v}{c}$

The orbital speed of the Earth is about  $3 \times 10^4$  m/s; therefore, the angle  $\theta$  is  $10^{-4}$  rad or 20.6 seconds of arc, with a total opening of  $2\theta = 41$  s as the Earth rotates—in agreement with Bradley's observation. The aberration reverses itself over the course of six months as the Earth orbits about the sun, in effect giving a circular motion to the star's position. This observation is in disagreement with the hypothesis of the Earth dragging the ether. If the ether were dragged with the Earth, there would be no need to tilt the telescope! The experimental observation of stellar aberration together with the null result of the Michelson and Morley experiment is enough evidence to refute the suggestions that the ether exists. Many other experimental observations have now been made that also confirm this conclusion.

The inability to detect the ether was a serious blow to reconciling the invariant form of the electromagnetic equations of Maxwell. There seems to be no single reference inertial system in which the speed of light is actually c. H. A. Lorentz and G. F. FitzGerald suggested, apparently independently, that the results of the Michelson-Morley experiment could be understood if length is contracted by the factor  $\sqrt{1 - v^2/c^2}$  in the direction of motion, where v is the speed in the direction of travel. For this situation, the length  $\ell_1$ , in the direction of motion, will be contracted by the factor  $\sqrt{1-v^2/c^2}$ , whereas the length  $\ell_2$ , perpendicular to v, will not. The result in Equation (2.3) is that  $t_1$  will have the extra factor  $\sqrt{1 - v^2/c^2}$ , making  $\Delta t$  precisely zero as determined experimentally by Michelson. This contraction postulate, which became known as the Lorentz-FitzGerald contraction, was not proven from first principles using Maxwell's equations, and its true significance was not understood for several years until Einstein presented his explanation. An obvious problem with the Lorentz-FitzGerald contraction is that it is an ad hoc assumption that cannot be directly tested. Any measuring device would presumably be shortened by the same factor.

# 2.3 Einstein's Postulates

At the turn of the twentieth century, the Michelson-Morley experiment had laid to rest the idea of finding a preferred inertial system for Maxwell's equations, yet the Galilean transformation, which worked for the laws of mechanics, was invalid for Maxwell's equations. This quandary represented a turning point for physics.

Albert Einstein (1879–1955) was only two years old when Michelson reported his first null measurement for the existence of the ether. Einstein said that he began thinking at age 16 about the form of Maxwell's equations in moving inertial systems, and in 1905, when he was 26 years old, he published his startling proposal\* about the principle of relativity, which he believed to be fundamental. Working without the benefit of discussions with colleagues outside his small circle of friends, Einstein was apparently unaware of the interest concerning the null result of Michelson and Morley.<sup>†</sup> Einstein instead looked at the problem in a more formal manner and believed that Maxwell's equations must be valid in

Albert Einstein (1879–1955), shown here sailing on Long Island Sound, was born in Germany and studied in Munich and Zurich. After having difficulty finding a position, he served seven years in the Swiss Patent Office in Bern (1902–1909), where he did some of his best work. He obtained his doctorate at the University of Zurich in 1905. His fame quickly led to appointments in Zurich, Prague, back to Zurich, and then to Berlin in 1914. In 1933, after Hitler came to power, Einstein left for the Institute for Advanced Study at Princeton University, where he became a U.S. citizen in 1940 and remained until his death in 1955. Einstein's total contributions to physics are rivaled only by those of Isaac Newton.

<sup>\*</sup>In one issue of the German journal *Annalen der Physik* **17**, No. 4 (1905), Einstein published three remarkable papers. The first, on the quantum properties of light, explained the photoelectric effect; the second, on the statistical properties of molecules, included an explanation of Brownian motion; and the third was on special relativity. All three papers contained predictions that were subsequently confirmed experimentally.

<sup>&</sup>lt;sup>†</sup>The question of whether Einstein knew of Michelson and Morley's null result before he produced his special theory of relativity is somewhat uncertain. For example, see J. Stachel, "Einstein and Ether Drift Experiments," *Physics Today* (May 1987), p. 45.

all inertial frames. With piercing insight and genius, Einstein was able to bring together seemingly inconsistent results concerning the laws of mechanics and electromagnetism with two postulates (as he called them; today we would call them laws). These postulates are

- 1. The principle of relativity: The laws of physics are the same in all inertial systems. There is no way to detect absolute motion, and no preferred inertial system exists.
- 2. The constancy of the speed of light: Observers in all inertial systems measure the same value for the speed of light in a vacuum.

The first postulate indicates that the laws of physics are the same in all coordinate systems moving with uniform relative motion to each other. Einstein showed that postulate 2 actually follows from the first one. He returned to the principle of relativity as espoused by Newton. Although Newton's principle referred only to the laws of mechanics, Einstein expanded it to include all laws of physics—including those of electromagnetism. We can now modify our previous definition of *inertial frames of reference* to be those frames of reference in which *all the laws of physics* are valid.

Einstein's solution requires us to take a careful look at time. Return to the two systems of Figure 2.1 and remember that we had previously assumed that t = t'. We assumed that events occurring in system K' and in system K could easily be synchronized. Einstein realized that each system must have its own observers with their own clocks and metersticks. An event in a given system must be specified by stating both its space and time coordinates. Consider the flashing of two bulbs fixed in system K as shown in Figure 2.6a. Mary, in system K' (the Moving system) is beside Frank, who is in system K (the Fixed system), when the bulbs flash. As seen in Figure 2.6b the light pulses travel the same distance in system K and arrive at Frank *simultaneously*. Frank sees the two flashes at the same time. However, the two light pulses do not reach Mary simultaneously, because system K' is moving to the right, and she has moved closer to the bulb on the right by the time the flash reaches her. The light flash coming from the left will reach her at some later time. Mary thus determines that the light on the right flashed before the one on the left, because she is at rest in her frame and both flashes approach her

#### Einstein's two postulates

# Inertial frames of reference revisited

#### **Simultaneity**



Figure 2.6 The problem of simultaneity. Flashbulbs positioned in system K at one meter on either side of Frank go off simultaneously in (a). Frank indeed sees both flashes simultaneously in (b). However, Mary, at rest in system K' moving to the right with speed v, does not see the flashes simultaneously despite the fact that she was alongside Frank when the flashbulbs went off. During the finite time it took light to travel the one meter, Mary has moved slightly, as shown in exaggerated form in (b).

#### at speed c. We conclude that

Two events that are simultaneous in one reference frame (K) are not necessarily simultaneous in another reference frame (K') moving with respect to the first frame.

We must be careful when comparing the same event in two systems moving with respect to one another. Time comparison can be accomplished by sending light signals from one observer to another, but this information can travel only as fast as the finite speed of light. It is best if each system has its own observers with clocks that are synchronized. How can we do this? We place observers with clocks throughout a given system. If, when we bring all the clocks together at one spot at rest, all the clocks agree, then the clocks are said to be **synchronized**. However, we have to move the clocks relative to each other to reposition them, and this might affect the synchronization. A better way would be to flash a bulb halfway between each pair of clocks at rest and make sure the pulses arrive simultaneously at each clock. This will require many measurements, but it is a safe way to synchronize the clocks. We can determine the time of an event occurring far away from us by having a colleague at the event, with a clock fixed at rest, measure the time of the particular event, and send us the results, for example, by telephone or even by mail. If we need to check our clocks, we can always send light signals to each other over known distances at some predetermined time.

In the next section we derive the correct transformation, called the **Lorentz transformation**, that makes the laws of physics invariant between inertial frames of reference. We use the coordinate systems described by Figure 2.1. At t = t' = 0, the origins of the two coordinate systems are coincident, and the system K' is traveling along the *x* and *x'* axes. For this special case, the Lorentz transformation equations are

Lorentz transformation equations  $x' = \frac{x - vt}{\sqrt{1 - v^2/c^2}}$  y' = y z' = z  $t' = \frac{t - (vx/c^2)}{\sqrt{1 - v^2/c^2}}$ (2.6)

**Relativistic factor** We commonly use the symbols  $\beta$  and the *relativistic factor*  $\gamma$  to represent two longer expressions:

$$\beta = \frac{v}{c} \tag{2.7}$$

$$\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$$
(2.8)

which allows the Lorentz transformation equations to be rewritten in compact form as

 $x' = \gamma(x - \beta ct)$  y' = y z' = z  $t' = \gamma(t - \beta x/c)$ (2.6)

Note that  $\gamma \ge 1$  ( $\gamma = 1$  when v = 0).

#### Synchronization of clocks

# 2.4 The Lorentz Transformation

In this section we use Einstein's two postulates to find a transformation between inertial frames of reference such that all the physical laws, including Newton's laws of mechanics and Maxwell's electrodynamics equations, will have the same form. We use the fixed system K and moving system K' of Figure 2.1. At t = t' = 0 the origins and axes of both systems are coincident, and system K' is moving to the right along the x axis. A flashbulb goes off at the origins when t = t' = 0. According to postulate 2, the speed of light will be c in both systems, and the wavefronts observed in both systems must be spherical and described by

$$x^2 + y^2 + z^2 = c^2 t^2 (2.9a)$$

$$x'^{2} + y'^{2} + z'^{2} = c^{2}t'^{2}$$
(2.9b)

These two equations are inconsistent with a Galilean transformation because a wavefront can be spherical in only one system when the second is moving at speed v with respect to the first. The Lorentz transformation *requires* both systems to have a spherical wavefront centered on each system's origin.

Another clear break with Galilean and Newtonian physics is that we do not assume that t = t'. Each system must have its own clocks and metersticks as indicated in a two-dimensional system in Figure 2.7. Because the systems move only along their *x* axes, observers in both systems agree by direct observation that

$$y' = y$$
$$z' = z$$

We know that the Galilean transformation x' = x - vt is incorrect, but what is the correct transformation? We require a linear transformation so that each event in system K corresponds to one, and only one, event in system K'. The simplest *linear* transformation is of the form

$$x' = \gamma(x - vt) \tag{2.10}$$

We will see if such a transformation suffices. The parameter  $\gamma$  cannot depend on x or t because the transformation must be linear. The parameter  $\gamma$  must be close to 1 for  $v \ll c$  in order for Newton's laws of mechanics to be valid for most of our measurements. We can use similar arguments from the standpoint of an observer stationed in system K' to obtain an equation similar to Equation (2.10).

$$x = \gamma'(x' + vt') \tag{2.11}$$

Because postulate 1 requires that the laws of physics be the same in both reference systems, we demand that  $\gamma' = \gamma$ . Notice that the only difference between Equations (2.10) and (2.11) other than the primed and unprimed quantities being switched is that  $v \rightarrow -v$ , which is reasonable because according to the observer in each system, the other observer is moving either forward or backward.

According to postulate 2, the speed of light is *c* in both systems. Therefore, in each system the wavefront of the flashbulb light pulse along the respective *x* axes must be described by x = ct and x' = ct', which we substitute into Equations (2.10) and (2.11) to obtain

$$ct' = \gamma(ct - vt) \tag{2.12a}$$



Figure 2.7 In order to make sure accurate event measurements can be obtained, synchronized clocks and uniform measuring sticks are placed throughout a system.

and

$$ct = \gamma(ct' + vt') \tag{2.12b}$$

We divide each of these equations by *c* and obtain

$$t' = \gamma t \left( 1 - \frac{v}{c} \right) \tag{2.13}$$

and

$$t = \gamma t' \left( 1 + \frac{v}{c} \right) \tag{2.14}$$

We substitute the value of t from Equation (2.14) into Equation (2.13).

$$t' = \gamma^2 t' \left( 1 - \frac{v}{c} \right) \left( 1 + \frac{v}{c} \right)$$
(2.15)

We solve this equation for  $\gamma^2$  and obtain

$$\gamma^2 = \frac{1}{1 - v^2 / c^2}$$

or

$$\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$$
(2.16)

In order to find a transformation for time t', we rewrite Equation (2.13) as

$$t' = \gamma \left( t - \frac{vt}{c} \right)$$

We substitute t = x/c for the light pulse and find

$$t' = \gamma \left( t - \frac{vx}{c^2} \right) = \frac{t - vx/c^2}{\sqrt{1 - \beta^2}}$$

We are now able to write the complete Lorentz transformations as

$$x' = \frac{x - vt}{\sqrt{1 - \beta^2}}$$

$$y' = y$$

$$z' = z$$

$$t' = \frac{t - (vx/c^2)}{\sqrt{1 - \beta^2}}$$
(2.17)

The inverse transformation equations are obtained by replacing v by -v as discussed previously and by exchanging the primed and unprimed quantities.

$$x = \frac{x' + vt'}{\sqrt{1 - \beta^2}}$$

$$y = y'$$

$$z = z'$$

$$t = \frac{t' + (vx'/c^2)}{\sqrt{1 - \beta^2}}$$
(2.18)

transformation equations

**Inverse Lorentz** 

Notice that Equations (2.17) and (2.18) both reduce to the Galilean transformation when  $v \ll c$ . It is only for speeds that approach the speed of light